hence Eq. (12) may be written in the form

$$S_T = S_S - \delta S$$

where δS is the difference in distance travelled in one cycle time between the two missiles. δS will be small in comparison to S_S , and may be evaluated approximately by binomial expansion, neglecting terms after the third. Hence,

$$\frac{S_T}{S_S} \approx 1 - \frac{(T_P - a - bV_{\rm I})}{kV_C b} \frac{\dot{m}\tau_P}{2M_0} \label{eq:state}$$

To simplify this expression, assume $V_1 \approx V_C$ and $a \ll T_P$. Hence,

$$S_T/S_S = 1 - [(k-1)/k]\delta M/2M_0$$
 (13)

where δM is the total change in mass during the pulse.

From Eq. (13) it may be seen that the fractional loss in distance or velocity of the pulsed missile is proportional to $\delta M/M_0$, which is the fractional change of mass during a pulse. Now k is the ratio T_P/T_C , and when k is large, (k-1)/k tends to unity. Hence, for large thrust ratios, the fractional loss of velocity is equal to half of the fractional change of mass during a pulse. As k tends towards unity (k-1)/k tends towards zero, and S_T approaches the values of S_S .

Equation (13) may be shown to be approximately equivalent to

$$S_T/S_S = 1 - \Delta V/2I_{SP}g$$

which is a more convenient form for calculation. For example, a change in velocity during a pulse of 500 ft/sec of a missile with an effective specific impulse of 250 lbf/lbm/sec results in a distance or velocity loss of

$$\delta S/S = 500/(2 \times 250 \times 32) \approx 3\%$$

Hence, in optimization of the velocity increment during a pulse, this effect will tend to favor small increments.

Reference

¹ Ullock, M. H., "Pulse Sustaining of Low-Altitude Cruise Missiles," *Journal of Spacecraft and Rockets*, Vol. 5, No. 10, Oct. 1968, pp. 1220–1221.

Reply by Author to A. J. Cruttenden

M. H. Ullock*

LTV Aerospace Corporation, Dallas, Texas

CRUTTENDEN has obtained a closed-form solution for the velocity and range covered by a missile during one cycle of pulse sustaining using a linear variation in drag with velocity. He identifies this solution as accounting for performance loss due to mass change during thrusting. It should be noted, however, that mass change is properly accounted for in the ideal velocity increment used in Ref. 1. The significant conclusion Cruttenden draws is that a large number of pulses is desired for maximum range. However, this conclusion can be misleading from a practical standpoint because of two simplifying assumptions implied by Cruttenden's analysis. These assumptions are: 1) thrust build-up and decay times during each pulse may be neglected; 2) the volume and weight of thermal barriers and ignitors for each pulse may be neglected.

Both of these assumptions are reasonable for a small number of pulses, but are invalid for a large number of short pulses. The method of Ref. 1 was used to conduct an analysis of the effect of the number of pulses on range considering only the weight and volume of barriers and ignitors. The

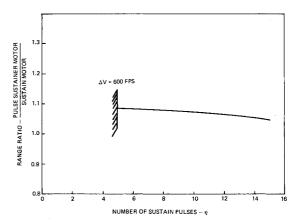


Fig. 1 Effect of the number of sustain pulses on range.

results shown on Fig. 1 indicate that a small number rather than a large number of pulses is desirable for maximum range. Including the effect of thrust build-up and decay would further magnify the decreasing trend with an increasing number of pulse.

Reference

¹ Ullock, M. H., "Pulse Sustaining of Low-Altitude Cruise Missiles," *Journal of Spacecraft and Rockets*, Vol. 5, No. 10, Oct. 1968, pp. 1220–1221.

Comments on "In Situ Vacuum Testing—A Must for Certain Elastomeric Materials"

Norman Fishman*
Stanford Research Institute, Menlo Park, Calif.

IN reporting their work on the effects of vacuum exposure on the properties of a solid rocket fuel, Mugler et al. state that their data demonstrate that significant changes in properties upon exposure to vacuum can occur even though weight loss is less than 1%. They further note that this finding is contrary to the general guidelines suggested by Muraca and Whittick.²

The work reported by Muraca and Whittick² is covered in much greater detail in earlier reports^{3,4} of research performed on the same program. These contain detailed results of in situ continuous and intermittent tests of a large number of elastomers and in situ constant load tests of several plastic materials. It can be generally concluded from our data that significant changes, other than chemorheological changes, occur only when accompanied by relatively large weight losses (>1%). Loss of weight in such materials is usually due to the irreversible outgassing of low-molecular-weight fragments, breakdown products, residual processing materials, and/or plasticizers or extenders. We also noted that re-exposure to the atmosphere did not result is recovery of properties to pre-exposure values.

In contrast to the essentially homogeneous materials examined in our program, the material studied by Mugler et al. is grossly heterogeneous. A composite solid propellant is highly filled with relatively large particles—particles that are loosely bound in the matrix. A process not occurring, or occurring only to a slight degree, in "homogeneous" materials can account for the behavior noted by the authors. The very small amount of interfacial moisture that influences

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^{*} Project Engineer, Missiles and Space Division. Associate Fellow AIAA.

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^{*} Senior Chemical Engineer. Associate Fellow AIAA.